# **Fifth Grade Overview**

#### **Operations and Algebraic Thinking (OA)**

- Write and interpret numerical expressions.
- Analyze patterns and relationships.

#### Number and Operations in Base Ten (NBT)

- Understand the place value system.
- Perform operations with multi-digit whole numbers and with decimals to hundredths.

#### Number and Operations—Fractions (NF)

- Use equivalent fractions as a strategy to add and subtract fractions.
- Apply and extend previous understandings of multiplication and division to multiply and divide fractions.

#### Measurement and Data (MD)

- Convert like measurement units within a given measurement system.
- Represent and interpret data.
- Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition.

#### Geometry (G)

- Graph points on the coordinate plane to solve real-world and mathematical problems.
- Classify two-dimensional figures into categories based on their properties.

#### Mathematical Practices (MP)

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

# **Fifth Grade: Mathematics Standards – Mathematical Practices – Explanations and Examples**

- In Grade 5, instructional time should focus on three critical areas: (1) developing fluency with addition and subtraction of fractions, and developing understanding of the multiplication of fractions and of division of fractions in limited cases (unit fractions divided by whole numbers and whole numbers divided by unit fractions); (2) extending division to 2-digit divisors, integrating decimal fractions into the place value system and developing understanding of operations with decimals to hundredths, and developing fluency with whole number and decimal operations; and (3) developing understanding of volume.
- (1) Students apply their understanding of fractions and fraction models to represent the addition and subtraction of fractions with unlike denominators as equivalent calculations with like denominators. They develop fluency in calculating sums and differences of fractions, and make reasonable estimates of them. Students also use the meaning of fractions, of multiplication and division, and the relationship between multiplication and division to understand and explain why the procedures for multiplying and dividing fractions make sense. (Note: this is limited to the case of dividing unit fractions by whole numbers and whole numbers by unit fractions.)
- (2) Students develop understanding of why division procedures work based on the meaning of base-ten numerals and properties of operations. They finalize fluency with multi-digit addition, subtraction, multiplication, and division. They apply their understandings of models for decimals, decimal notation, and properties of operations to add and subtract decimals to hundredths. They develop fluency in these computations, and make reasonable estimates of their results. Students use the relationship between decimals and fractions, as well as the relationship between finite decimals and whole numbers (i.e., a finite decimal multiplied by an appropriate power of 10 is a whole number), to understand and explain why the procedures for multiplying and dividing finite decimals make sense. They compute products and quotients of decimals to hundredths efficiently and accurately.
- (3) Students recognize volume as an attribute of three-dimensional space. They understand that volume can be measured by finding the total number of same-size units of volume required to fill the space without gaps or overlaps. They understand that a 1-unit by 1-unit by 1-unit cube is the standard unit for measuring volume. They select appropriate units, strategies, and tools for solving problems that involve estimating and measuring volume. They decompose three-dimensional shapes and find volumes of right rectangular prisms by viewing them as decomposed into layers of arrays of cubes. They measure necessary attributes of shapes in order to determine volumes to solve real world and mathematical problems.

<b>Operations and Algeb</b>	braic Thinking	g (OA)					
Write and interpret nu	umerical expres	ssions					
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.OA.1 Use parenthe brackets, or braces in numerical expression and evaluate express with these symbols. Connection: 5.OA.2	eses, n brack inclu brack ins, ions Evalua using oper- using	·	This standard start learning expressions to when and ho with whole r and divide do <b>Examples:</b> • (26 - • $\{[2x]$ • 12 - • (2 + • 6-( • {80 To further do operations, s they compary <b>Examples:</b> • 15 - • 3 x • 24 ÷	s and Examples d builds on the expension g the conventional of that use grouping sy- that use grouping sy-	rder. Students need mbols throughout t s, brackets, and bra ymbols can be used (23-18)] An (23-18)] A	l experiences with n the year to develop aces. First, students d as students add, su nswer: 11 nswer: 32 nswer: 11.2 nswer: 5 nswer: 5 1/6 Answer: 10 ping symbols and fa ations to make the o tly.	are expected to nultiple understanding of use these symbols obtract, multiply 08 acility with equations true or

<b>Operations and Algel</b>		ng (OA)					
Analyze patterns and				I			
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.OA.3 Generate two numerical patterns u two given rules. Idem apparent relationshi between correspondi terms. Form ordered consisting of corresponding terms two patterns, and gra the ordered pairs on coordinate plane. Fo example, given the ru "Add 3" and the start number 0, and the giv rule "Add 6" and the starting number 0, ge the terms in the result sequences, and obser the terms in one sequences the terms in the other sequence. Explain informally why this is Connections: 5.RI.3; 5.W.2 5.SL.1	Gen pa singGen pa giusinggitifyFor pspscoingcol pairsfoaAna coaAna correclecotingthvenpanerate tingthence ondingon	gets herate two numerical atterns using two ven rules. m ordered pairs onsisting of presponding terms or the two patterns. uph generated rdered pairs on a pordinate plane. alyze and explain the lationships between prresponding terms in e two numerical atterns.	Example: • Use t write • Use t 0, 6, After co sequence this is b mathem sequence added of sequence betweet 0 (0) 0 (0) 0 (1) 0 (2) 0	the rule "add 6" to w 12, 18, 24, omparing these two ce is twice the corres by describing the path natical notation (See ces start with zero an 6, which is twice as n ce. Students may als n the two numerical 0, $^{+3}$ 3, $^{+3}$ 6, 0, $^{+6}$ 6, $^{+6}$ 12, tudents can describe onding terms of the aphed on a coordinat	write a sequence of magnetic as equences, the stude sponding terms of the terms. The example below). And to generate each to use the distributive patterns by reasonine $^{+3}9$ , $^{+3}12$ , $^{+6}18$ , $^{+6}24$ , that the second seque first sequence, the term of the second que the term of the term of the second que the term of term	umbers. Starting with nts notice that each to e first sequence. One heir justification may student may explain erm of the second se o produce the terms e property to describe g that $6 + 6 + 6 = 2$ of the second se to the terms e property to describe g that $6 + 6 + 6 = 2$ of the second se to the terms of the terms is the terms can be written in recognize that each	h 0, students write term in the second e way they justify y include some that both quence he/she in the first e the relationship (3 + 3 + 3). write the n ordered pairs and point on the graph

Number and Operati	ons in Base T	en (NBT)							
Understand the place v	alue system								
Understand the place v Make sense of problems and persevere in solving them. <u>Standards</u> Students are expected to: <b>5.NBT.1 Recognize</b> that in a multi-digit number, a digit in on place represents 10 times as much as it represents in the place	ralue systemReasonabstractly andquantitatively.TargetsRecognizmulti-dia digit irepresenas muchrepresenas muchrepresenas muchrepresenas muchrepresenas muchrepresen	Construct viable arguments and critique the reasoning of others.e that in a igit number, n one place nts 10 times n as itExplan In four stand pictur place fracti Before digit and 1 A study	ard extends this res of base ten b value relationsh onal language to considering the whole numbers, /10 of what it re	s examined the relation understanding to the locks, and interactive hips. They use their un describe those composition relationship of deciminal a digit in one place re- presents in the place	relationship of decim images of base ten b inderstanding of unit f arisons. al fractions, students epresents 10 times wh to its left.	Look for and make use of structure. in numbers for whole hal fractions. Students locks to manipulate a fractions to compare of express their underst hat it represents in the ns place (5555) repre-	use base ten blocks, nd investigate the lecimal places and anding that in multi- place to its right		
to its right and 1/10 of what it represents in the place to its left. Connections: 5.NBT.2; 5.RI.3; 5.W.2d $A = 1/10 \text{ for what it represents in the place to its left.}$ A student thinks, "I know that in the number 5555, the 5 in the tens place (5555) represents 500. So a 5 in the hundreds place is ten times tens place (5555) represents 500. So a 5 in the hundreds place. To extend this understanding of place value to their work with decimals, students use they cut it into 10 equal pieces, shade in, or describe 1/10 of that model using fraction is 1 out of 10 equal parts. So it is 1/10". I can write this using 1/10 or 0.1"). They refinding 1/10 of a 1/10 (e.g., dividing 1/10 into 10 equal parts to arrive at 1/100 or 0 their reasoning, "0.01 is 1/10 of 1/10 thus is 1/100 of the whole unit." In the number 55.55, each digit is 5, but the value of the digits is different because of <b>5 5 1 5 5 1 5 5 1 5 1 5 1 1 1 1 1 1 1 1 1 1</b>							s much as a 5 in the a model of one unit; nal language ("This eat the process by 1) and can explain the placement. The 5 in the ones		
			The 5 that the arrow points to is 1/10 of the 5 to the left and 10 times the 5 to the right. The 5 in the ten place is 10 times five hundredths. $ \begin{array}{c}                                     $						

Number and Operati	ons in I	Base Te	en (NBT)											
Understand the place	value sy	stem												
Make sense of problems	Reason		Construct viable	Model with	Use appropriate	Attend to precision.	Look for and make	Look for and						
and persevere in solving them.	abstract quantita	•	arguments and critique the reasoning of others.	mathematics.	tools strategically.		use of structure.	express regularity in repeated reasoning.						
Standards	quantita	Target		Explanations and Examples										
Students are expected to:			sent powers of 10	Examples:										
5.NBT.2 Explain patt	<b>5.NBT.2 Explain patterns</b>   using whole number		-											
in the number of zeros of exponents.		• St	udents might write:											
the product when		-	ly translate between	36	$x 10 = 36 x 10^{1} = 3$	60								
	multiplying a number by				x 10 x 10 = 36 x 10	$0^2 = 3600$								
powers of 10, and exp		-	aised to a whole		x 10 x 10 x 10 = 36									
patterns in the placen		num	per exponent, the			2								
<b>–</b>	of the decimal point when a decimal is multiplied or expanded form, and			36	$36 \ge 10 \ge 10 \ge 10 \ge 10 \ge 36 \ge 10^4 = 360,000$									
divided by a power of			lard notation	• Students might think and/or say: I noticed that every time, I multiplied by 10 I added a zero to the end of the										
Use whole-number		``	= 10 x 10 x 10 =											
exponents to denote		1000	/		e 10 times larger.									
powers of 10.		-	n the patterns in the	To make a digit 10 times larger, I have to move it one place value to the lef										
		number of zeros of the		When I multiplied 36 by 10, the 30 became 300. The 6 became 60 or the										
Connections: 5.NBT.1; 5.R 5.W.2b	?1.3;	-	uct when multiplying nber by powers of		epresent 3 one-									
5.00.20		10.	nder by powers of	hu	hundreds (instead of 3 tens) and the 6 represents 6 tens (inst									
			n the relationship of	• St	udents should be abl	le to use the same ty	vpe of reasoning as	above to explain						
		-	lacement of the		ny the following mu	•		*						
		-	nal point when a		nse.	*								
			nal is multiplied or	54	$23 \times 10^3 = 522000$	The place value of	572 is increased by	$r^{2}$ places						
	divided by a power of 10.				$523 \times 10^3 = 523,000$ The place value of 523 is increased by 3 pl									
					$223 \times 10^2 = 522.3$	The place value of	5.223 is increased b	by 2 places.						
				52	$52.3 \div 10^1 = 5.23$ The place value of 52.3 is decreased by one place.									

Number and Operation	ons in Base Te	en (NBT)									
Understand the place v	alue system										
Make sense of problems	Reason	Construct viable		Model with	Use appropriate	Attend to precision.	Look for and make	Look for and			
and persevere in solving them.	abstractly and quantitatively.	arguments and c the reasoning of		mathematics.	tools strategically.		use of structure.	express regularity in repeated reasoning.			
<u>Standards</u>	<u>Targets</u>		Explanations and Examples								
Students are expected to:	Read and	write				veloped in fourth grad					
5.NBT.3 Read, write	uccilliai	to				ences with using deci					
and compare decima	ls thousand	dths using				They use concrete mo s. Models may includ					
to thousandths:	base-ten	numerals,				hnology-based, etc. T					
a. Read and write	number	names, and				rm, as well as in expa					
decimals to	expande	ed form.			s them to understandi	ng equivalence of dec	cimals $(0.8 = 0.80 = 0.00)$	.800).			
thousandths using	Use >, =,	and <	Example:								
base-ten numerals,	symbols	to record	• Some equivalent forms of 0.72 are:								
number names, and	the result	lts of	72/100								
expanded form,	compari	sons	$7/10 + 2/100$ $0.720$ $7 \ge (1/10) + 2 \ge (1/100) + 2 \ge (1/100) + 0 \ge (1/1000)$ $(1/102)$								
e.g., $347.392 = 3 \times 10$	0 between	decimals.									
$+4 \times 10 + 7 \times 1 + 3 \times$	Compare	two		(1/100)		720/1000					
$(1/10) + 9 \times (1/100) +$	2 decimal	s to the	C . 1	0.70 + 0.02							
× (1/1000).	thousan	dths based				mal numbers and related the second related to the second relation tot to the second relatio					
b. Compare two	on the p	lace value				r understanding of fra					
decimals to	of each	digit.	Examp	-		C	1				
thousandths based of	n		٠			t might think, "25 hur					
meanings of the digit						dredths more. They n		ison as $0.25 > 0.17$			
in each place, using >			•			other way to express		so I need to			
=, and < symbols to	,		• Comparing 0.207 to 0.26, a student might think, "Both numbers have 2 tenths, so I need to compare the hundredths. The second number has 6 hundredths and the first number has no								
record the results of			hundredths so the second number must be larger. Another student might think while writing								
comparisons.						thousandths (and ma					
-				· ·	,	so think of it as 260 t	housandths (260/100	0). So, 260			
Connections: 5.RI.5; 5.SL.6				thousandths is	more than 207 thous	andths.					

Number and Operati	ons in l	Base Te	en (NBT)						
Understand the place	value sy	stem							
Make sense of problems and persevere in solving them.		•	Construct viable arguments and critique the reasoning of others.		Nodel with nathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Students are expected to: 5.NBT.4 Use place v understanding to r decimals to any pla	bersevere in solving a.abstractly and quantitatively.arguments and critique the reasoning of others.rdards ts are expected to:Targets Use knowledge of base ten and place value to round decimals to any place.Image: standing to round				When rou possible given nu Example: • Ro Stud eit	ns and Examples nding a decimal to answers, and use to mber to the possib ound 14.235 to the lents recognize tha her 14.2 or 14.3. T 4.20) than to 14.3	their understandin ble answers. nearest tenth. at the possible ans They then identify	g of place value to wer must be in ter	ths thus, it is

Number and Operati	ions in I	Base Te	en (NBT)							
Perform operations with multi-digit whole numbers and with decimals to hundredths										
Make sense of problems and persevere in solving them.	Reason abstractly and guantitatively.		Construct viable arguments and critique the reasoning of others.	Model with mathematic	Use approp s. tools strate		Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.	
Standards Students are expected to: 5.NBT.5 Fluently multiply multi-digi whole numbers usi the standard algor	ing	digit using	<u>s</u> ly multiply multi- whole numbers g the standard ithm.	<ul> <li><u>Explanations and Examples</u></li> <li>In prior grades, students used various strategies to multiply. Students can continue to use these different strategies as long as they are efficient, but must also understand and be able to use the standard algorithm. In applying the standard algorithm, students recognize the importance of place value.</li> <li><b>Example</b>:</li> <li>123 x 34. When students apply the standard algorithm, they, decompose 34 into</li> </ul>						
	30 + 4. Then they multiply 123 by 4, the value of the number in the ones place and then multiply 123 by 30, the value of the 3 in the tens place, and add the two products.									

Number and	<b>Operations in</b>	Base Ten	(NBT)
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Perform operations with multi-digit whole numbers and with decimals to hundredths

Perform operations with	ui muiti-aigit v	vilole number	s and w	iui uecimais i	o nunui eutits						
Make sense of problems	Reason	Construct viable		Model with	Use appropriate	Attend to precision.	Look for and make	Look for and			
	abstractly and	arguments and	•	mathematics.	tools strategically.		use of structure.	express regularity in			
them.	quantitatively.	the reasoning of						repeated reasoning.			
<u>Standards</u>	<u>Targets</u>		Explanations and Examples								
Students are expected to:	Find whole-	number	In fourth grade, students' experiences with division were limited to dividing by one-digit divisors. This standard extends students' prior experiences with strategies, illustrations, and explanations. When the two-digit divisor is a "familiar" number, a student might decompose the dividend using place value. <b>Example</b> :								
5.NBT.6 Find whole-	quotients of	of whole									
number quotients of	numbers v	with up to									
whole numbers with	four-digit	dividends	Examp •		ad notation 2682 ·	25 = (2000 + 600 + 8)	(1 + 2) + 25				
up to four-digit	and two-d			• •							
dividends and two-	divisors.	-0	•			ne relationship betwee					
digit divisors, using		es based on			ed by 25 has to be 24	is 4 so 200 divided by	y 25 is 8 and 2000 div	vided by 25 is 80.			
strategies based on	place valu				2	80 divided by 25 is 3	with a reminder of 5	(Note that a			
place value, the	-	-			ight divide into 82 an		with a reminder of 5				
properties of	properties				6	the 5 leaves a remain	nder of 7.				
operations, and/or	-	, and/or the	<ul> <li>80 + 24 + 3 = 107. So, the answer is 107 with a remainder of 7.</li> <li>Using an equation that relates division to multiplication, 25 x n = 2682, a student might estimate</li> </ul>								
the relationship		p between									
between	multiplica		the answer to be slightly larger than 100 because s/he recognizes that $25 \times 100 =$								
	division to			2500.							
multiplication and	division p	roblems.	٠	Example: 968							
division. Illustrate	Illustrate an	d explain				represent 962 and use					
and explain the	division ca	alculations			ders are not part of th	nues to make the array	y until no more group	os of 21 can be			
calculation by using	by using e	quations,		maue. Reillain	21	ic array.					
equations,	rectangula	-			10						
rectangular arrays,	and/or are	-			10						
and/or area models.		u 11100015.									
					10						
			6								
						Conti	inued on payt page				
						Conti	nued on next page				

Number and Operation	ions in Base T	en (NBT)											
Perform operations w	Perform operations with multi-digit whole numbers and with decimals to hundredths <i>continued</i>												
Make sense of problems and persevere in solving	Reason abstractly and	Construct viable arguments and critique	Model wi mathema	-	Use appropriate	Attend to precision.	Look for and make use of structure.	Look for and express regularity in					
them.	quantitatively.	the reasoning of others.	mathema	itics.	tools strategically.		use of structure.	repeated reasoning.					
<u>Standards</u> Students are expected to:	<u>Targe</u>	<u>ts</u>			ns and Examples								
5.NBT.6. continued			Exan	npie:	9984 ÷ 64								
• An area model for division is shown below. As the student uses the area													
	model, s/he keeps track of how much of the 9984 is left to divide.												
				<u> </u>	54	64 9984							
			100	64	100	<u>-6400</u> (100 × 0 3584	64)						
			100	~	100	-3200 (50 × 6	4)						
			50		200	384							
			50	32	200	<u>-320</u> (5 × 64) 64	)						
			5	3	320	-64 (1 × 64	)						
			1		64	0	~						

Number and Operation	ons in Base Te	en (NBT)					
Perform operations wi	th multi-digit <b>v</b>	whole numbers and w	ith decimals t	o hundredths			
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.Use appropriate tools strategically.Attend to precision.Look for and make use of structure.Look for and express regula repeated reas				
Students are expected to: 5.NBT.7 Add, subtra multiply, and divide decimals to hundred using concrete model drawings and strateg based on place value, properties of operation and/or the relationsh between addition and subtraction; relate the strategy to a written method and explain the reasoning used. Connections: 5.RI.3; 5.W.2 5.W.2c; 5.SL.2; 5.SL.3	and ahundths,concls ordrawgiesbasedpropons,and/aipbetwlsubtrneRelatewritttheexplaoperation	<u>s</u> ubtract, multiply, livide decimals to redths using rete models or ings and strategies d on place value, erties of operations, or the relationship een addition and faction. the strategy to a en method and ain the reasoning to solve decimal ation calculations.	This standard whole num answers, the the value of <b>Examples:</b> • $3.6 +$ • $4$ • $5.4 -$ • $4$ • $5.4 -$ • $6 \times 2$ • $4$ • $6 \times 2$ • $4 $	bers in grades 1-4 t ey should estimate f the numbers. - 1.7 A student might esti- han 3 $\frac{1}{2}$ and 1.7 is f - 0.8 A student might esti- number less than 1 is 2.4 A student might esti- 5 x 3 is 18. Another because s/he figures and think of 2 $\frac{1}{2}$ gro uld be able to expre- dths to hundredths. ch other), it is impor- ch other. This unde- their understanding	o decimal values. B answers based on the more than 1 <sup>1</sup> / <sub>2</sub> . Imate the answer to a being subtracted. Imate an answer bet student might give the answer to be very oups of 6 as 12 (2 gr stat when they a So, when they are a rtant that they write rstanding can be reig of addition of fract a standard in fourth	s and strategies they before students are a neir understanding of larger than 5 becau be a little more that tween 12 and 18 sin an estimate of a little roups of 6) + 3 ( $\frac{1}{2}$ of dd decimals they ad adding in a vertical numbers with the s inforced by connect etions. Adding fraction	sked to give exact of operations and se 3.6 is more in 4.4 because a ce $6 \ge 2$ is 12 and le less than 15 er than $6 \ge 2\frac{1}{2}$ of a group of 6). Id tenths to tenths format (numbers ame place value ing addition of

Number and Operati Perform operations w			ith decimals (	a hundredths cont	tinuad				
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.		
and persevere in solving	abstractly and quantitatively.	arguments and critique the reasoning of others.	mathematics. Explanation Example: • 3 t ter [ The Example: ************************************	tools strategically.	From 4 wholes. The 7/10  or  3.7. an be useful for ill 1.3 2.4 ble to describe the mple, 2/100. r $60/100.$ 0 or $40/100.$ ber in each group encouraged to app	use of structure. e wholes must be ustrating products 2.4 $\times 1.3$ .12 .60 .40 $\pm 2.00$ 3.12 partial products d or share ly a fair sharing n	express regularity in repeated reasoning. divided into s. s.		
			0.6 0.6 0.6 0.6 Continued on next page						

Number and Operati	ons in Base Te	en (NBT)									
Perform operations with	ith multi-digit v	whole numbers and w	ith decimals (	to hundredths cont	inued						
Make sense of problems	Reason	Construct viable	Model with	Use appropriate	Attend to precision.	Look for and make	Look for and				
and persevere in solving	abstractly and	arguments and critique	mathematics.	tools strategically.		use of structure.	express regularity in				
them.	quantitatively.	the reasoning of others.					repeated reasoning.				
<u>Standards</u> Students are expected to:	<u>Target</u>	<u>s</u>		Explanations and Examples Example: Find the number of groups							
5.NBT.7. continued			Example:	<b>Example:</b> Find the number of groups							
5.NB1.7. conunuea			lor	<ul> <li>Joe has 1.6 meters of rope. He has to cut pieces of rope that are 0.2 meters long. How many can he cut?</li> <li>To divide to find the number of groups, a student might: <ul> <li>draw a segment to represent 1.6 meters. In doing so, s/he would count in tenths to identify the 6 tenths, and be able identify the number of 2 tenth within the 6 tenths. The student can then extend the idea of counting by tenths to divide the one meter into tenths and determine that there are 5 more groups of 2 tenths.</li> <li>1.6 m</li> </ul> </li> </ul>							
			<ul> <li>     () () () () () () () () () () () ()</li></ul>								
			Technolog SMART N		ate models using Int	teractive Whiteboar	rd software (such as				

Number and Operati	ons—Fra	ctions	s (NF)					
Use equivalent fractio	ns as a stra	ategy	to add and subtract	fractions				
Make sense of problems and persevere in solving them. <u>Standards</u> <u>Students are expected to:</u> <b>5.NF.1 Add and sub</b> fractions with unlike denominators (inclu mixed numbers) by replacing given fract in such a way as to produce an equivale	and persevere in solving hem.abstractly and quantitatively.arguments and critique the reasoning of others.andards andards udents are expected to:TargetsNF.1 Add and subtract actions with unlike enominators (including ixed numbers) by eplacing given fractions such a way as toTargetsGenerate equivalent fractions to find the like denominator.Solve addition and subtraction problems involving fractions (including mixed		Model with mathematics. Explanatic Students a fourth gra common will alway denomina Examples:		y to rewrite fraction by should know the denominator but i	ons in an equivale at multiplying the	nt form to find denominators	
sum or difference of fractions with like denominators. For example, $2/3 + 5/4 =$ + 15/12 = 23/12. (In general, $a/b + c/d =$ ( bc)/bd) Connection: 5.NF.2	The difference of the unlike denominators the unlike denominators unlike denominators unlike denominators using an equivalent fraction strategy. $3\frac{1}{4} - \frac{1}{6} = 3\frac{3}{12} - \frac{2}{12} = 3\frac{1}{12}$ $3\frac{1}{4} - \frac{1}{6} = 3\frac{3}{12} - \frac{2}{12} = 3\frac{1}{12}$							

Number and Operations	-Fraction	is (NF)	0-00					
Use equivalent fractions as	s a strategy	to add and su	ıbtract fi	ractions				
	son tractly and ntitatively.	Construct viable arguments and the reasoning o	critique	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
StandardsStudents are expected to:5.NF.2 Solve wordproblems involvingaddition andsubtraction of fractionsreferring to the samewhole, including cases ofunlike denominators,e.g. by using visualfraction models orequations to representthe problem. Usebenchmark fractionsand number sense offractions to estimatementally and assess thereasonableness ofanswers. For example,recognize an incorrectresult 2/5 + 1/2 = 3/7, byobserving that 3/7<1/2.Connections: 5.NF.1; 5.RI.7;5.W.2c; 5.SL.2; 5.SL.3	Targets Generate fractions denomin Solve wor involvin and subt fractions unlike denomin referring same wh using vi models to repres problem Evaluate reasonal an answ fractions	equivalent s to find like nators. rd problems ag addition traction of s with nators g to the nole (e.g. by sual fraction or equations sent the h). the pleness of er, using al number		Jerry was make other needed <sup>2</sup> Mental estimat A student may explanation may total must be n cannot be more	ing two different typ /3 cup of sugar. How ion: say that Jerry needs ay compare both fraction to re than 1. In addition te than 2. tea model $\frac{2}{3}$ cup of sugar $\frac{2}{3} = \frac{8}{12}$ $\frac{3}{4}$	w much sugar did more than 1 cup ctions to $\frac{1}{2}$ and st on, both fraction $+\frac{2}{3} = \frac{17}{12} = \frac{12}{12} + \frac{5}{12}$	he need to make bo of sugar but less that ate that both are larg s are slightly less that	cup of sugar and the th recipes? an 2 cups. An ger than ½ so the

Number and Operati	ions—Fraction	s (NF)	)					
Use equivalent fractio	ons as a strategy	to add	d and subtract i	fractions <i>cont</i>	inued			
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	argum	ruct viable nents and critique asoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
them. <u>Standards</u> Students are expected to: <b>5.NF.2.</b> continued	quantitatively. <u>Targets</u>	the real	Explanations a Example: Usin • Sonia I much v • If Mary the firs $\circ$ Us $\circ$ A mit Example: Usin • This m 1 + 3/1 $3^{1/6}$ a Once • This di	g a bar diagram had 2 1/3 candy will she have le y ran 3 miles ev t week she ran sing addition to student might a les + 1/6 of a n g an area mode odel shows 1 $\frac{3}{2}$ 2 + 2/12 = 1 5	h v bars. She promised ft after she gives her very week for 4 week 1 <sup>3</sup> ⁄ <sub>4</sub> miles. How mar find the answer:1 <sup>3</sup> ⁄ <sub>4</sub> add 1 <sup>1</sup> ⁄ <sub>4</sub> to 1 <sup>3</sup> ⁄ <sub>4</sub> to get nile is what Mary nee el to subtract 4 subtracted from 3 1	brother the amount as, she would reach 1 by miles does she sti + n = 3 to 3 miles. Then he eds to run during that /6 leaving $1 + \frac{1}{4} + 1$ 1 1 1 1 1 1 1 1 1	she promised? her goal for the month ll need to run the first or she would add 1/4 tt week. 1/6 which a student c 2 - 1 9/12 = 1 5/12. expressed with a der h, 2 14/12 - 1 9/12 =	f a candy bar. How th. The first day of st week? 6 more. Thus 1 <sup>1</sup> /4 can then change to nominator of 12.

Number and Operati	ions—Fraction	s (NF)								
Use equivalent fractio	ons as a strategy	to add and subtract	fractions <i>cont</i>	inued						
Make sense of problems	Reason	Construct viable	Model with	Use appropriate	Attend to precision.	Look for and make	Look for and			
and persevere in solving	abstractly and	arguments and critique	mathematics.	tools strategically.		use of structure.	express regularity in			
them.	quantitatively.	the reasoning of others.					repeated reasoning.			
<u>Standards</u>	<u>Target</u>	<u>s</u>		Explanations and Examples						
Students are expected to:				Estimation skills include identifying when estimation is appropriate, determining the						
5.NF.2. continued			level of ac	curacy needed, selec	cting the appropriate	e method of estimat	tion, and verifying			
			solutions or determining the reasonableness of situations using various estimation							
			strategies. Estimation strategies for calculations with fractions extend from students'							
			work with whole number operations and can be supported through the use of physical							
			models.							
			Example:							
			-	3		1				
			• Elli drank 5 quart of milk and Javier drank 10 of a quart less than Ellie. How							
				-		-				
			mı	ch milk did they dr	ink all together?					
				lution:	and the collection of					
				$\frac{1}{2} = \frac{6}{2} - \frac{1}{2} = \frac{5}{2}$	L This is how much	h milk Javier drank				
			5	10 10 10 10	0					
			3	5 6 5 1	1					
			$\frac{3}{5} + \frac{5}{10} = \frac{6}{10} + \frac{5}{10} = \frac{11}{10}$ Together they drank $1\frac{1}{10}$ quarts of milk							
				10 10 10 1		10 -				
			This soluti	on is reasonable bec	ause Ellie drank me	ore than ½ quart an	d Javier drank ½			
				gether they drank sl		•	a su fier druine /2			
			qualt so to	Section they drank st	ignery more than on	ic quui t.				

Number and Operati	ons—Fraction	ns (NF)						
Apply and extend pre-	vious understai	ndings of multiplication	on an	nd divisio	n to multiply and o	divide fractions		
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.		lel with hematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.NF.3 Interpret a fra division of the numera the denominator (a/b Solve word problems involving division of w numbers leading to an in the form of fraction mixed numbers, e.g., k visual fraction models equations to represent problem. For example interpret 3/4 as the rest dividing 3 by 4, noting multiplied by 4 equals that when 3 wholes are equally among 4 peopl person has a share of s If 9 people want to sha pound sack of rice equ weight, how many pour rice should each person Between what two who numbers does your ans Connection: 5.SL.1	ction as itor by $= a \div b$ ).div by $a \div$ whole iswersSolve investoris orwhole investoris orwhole investororfra fra theorfra fra eq that 3/4orfra eq pro- fra that 3/4orfra eq pro- fra 	rpret a fraction as rpret a fraction as vision of the numerator the denominator (a/b ÷ b). we word problems volving division of nole numbers leading swers in the form of actions or mixed umbers. (e.g. using sual fraction models of uations to represent the oblem). rpret the remainder as actional part of the oblem.	to br he	Students drawin multipl sharing Example • 7 • 7 • 7 • 7 • 7 • 7 • 7 • 7 • 7 • 7	Ten team members each student get? • When working are being divide following equat which can also	aining their thinking ad 3/5 as "three fifth at 3/5 can also be in are sharing 3 boxes this problem a stude ed into 10 groups, se ion, 10 x $n = 3$ (10) be written as $n = 3$ - into 10 groups, res bs are having pizza pizzas for every 5 s pizzas for every 8 s decide which party y? If you want to h classrooms have a to ch classroom receiv as a whole number problem as <sup>27</sup> / <sub>6</sub> . Th	g when working with hs" and after many interpreted as "3 divi- of cookies. How m ent should recogniz to s/he is seeing the groups of some amo- ÷ 10. Using models ulting in each team parties. For the Ma students. For the Ma students. Since you to attend. How ma ave the most pizza, ptal of 27 boxes of p e? division problem to ey explain that each	h fractions in experiences with ded by 5." huch of a box will e that the 3 boxes solution to the ount is 3 boxes) or diagram, they member getting hth Club, the ident council, the are in both uch pizza would which party pencils. How

Number and Operatio	ons—Fraction	is (NF)									
Apply and extend previ	ious understa	ndings of multiplicati	on and di	vision	to multiply and	divide fraction	IS				
	Reason	Construct viable	Model wit	h I	Use appropriate	Attend to	Look for and make	Look for and express			
	abstractly and	arguments and critique	mathemat	tics.	tools strategically.	precision.	use of structure.	regularity in repeated			
	quantitatively.	the reasoning of others.			reasoning.						
<u>Standards</u>		<u>Targets</u>			anations and Exan						
Students are expected to:		Find area of a rec	•	Students are expected to multiply fractions including proper fractions, improper fractions, and mixed numbers. They multiply fractions efficiently and accurately							
5.NF.4 Apply and exte	-		with fractional side								
understandings of mul		lengths using different			1		xtual and non-contextu				
multiply a fraction or		strategies. (e.g.,	tiling		• •	•	as $3/5 \ge 6$ , they can the	nink of the operation			
number by a fraction.		with unit square	s of the		in more than or $2 \times (6 \div 5) \circ r$						
a. Interpret the produce		appropriate unit	fraction		$3 \times (6 \div 5) \text{ or } ($						
a parts of a partition of	of q into b	side lengths,			$(3 \times 6) \div 5$ or $18 \div 5$ (18/5)						
equal parts; equivalen	qual parts; equivalently, as a result multiplying side				• Students create a story problem for 3/5 x 6 such as: Isabel had 6 feet of wrapping paper. She used 3/5 of the paper to wrap						
of a sequence of opera	a sequence of operations $a \times q / b$ . lengths).			some presents. How much does she have left?							
For example, use a visi	<i>or example, use a visual fraction</i> Represent fraction				1		. How far did he run a	fter 6 days?			
model to show $(2/3) \times 4$	4 = 8/3, and	products as recta	angular		(Interpreting th			liter o duys.			
create a story context f	or this	areas.	C	Examples: Building on previous understandings of multiplication							
equation. Do the same	with (2/3) ×	Justify multiplyin	g	• Rectangle with dimensions of 2 and 3 showing that $2 \times 3 = 6$ .							
(4/5) = 8/15. (In general	al, $(a/b) \times (c/d)$		0		C	F	2				
= ac/bd.		to find the area		T							
b. Find the area of a re	ectangle with	same as tiling a				3					
fractional side lengths	0	rectangle with u	nit								
with unit squares of th		•	ŕ			1					
unit fraction side lengt		- 1	fraction			L	= 1				
that the area is the san		side lengths.			• Rectangle with	n dimensions of	12 and $2/3$ showing the function of the fu	hat 2 x $2/3 = 4/3$			
		Model the area of	·			⊢	-				
• • •	e found by multiplying the sideModel the area ofngths. Multiply fractional siderectangles with					$\frac{2}{2}$ T					
	engths to find areas of rectangles, fractional side lengths					3 -					
8	and represent fraction products as with unit squares to										
rectangular areas					= 1						
Connections:5.RI.3; 5.W.2b	h. 5 W/ 2d. 5 SI 1		L	Continued on next page							
Connections.3.Ki.3, 5.W.20	,vv.zu,SL.1	rectangles.									

Number and Operati	ions—Fraction	s (NF)									
Apply and extend pre	vious understar	ndings of multiplication	on and divisio	n to multiply and o	livide fractions <i>col</i>	ntinued					
Make sense of problems	Reason	Construct viable	Model with	Use appropriate	Attend to precision.	Look for and make	Look for and				
and persevere in solving	abstractly and	arguments and critique	mathematics.	tools strategically.		use of structure.	express regularity in				
them.	quantitatively.	the reasoning of others.					repeated reasoning.				
<u>Standards</u> Students are expected to:	<u>Target</u>	<u>s</u>		ons and Examples							
5.NF.4. continued			$\circ  2\frac{1}{2} \text{ groups of } 3\frac{1}{2}$								
J.M. H. Commucu				3 <sup>1</sup>							
		$2\frac{1}{2}$ 1 1 1 $\frac{1}{2}$									
				$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$							
			±.								
			Inc	$a_{1}$ and $b_{2}$ and $b_{3}$	u 4 studente uco en e	ma madal ta vigualia	ait as a 2 by 4 amor				
				olving the problem $\frac{4}{3}$							
				f small rectangles each $(5 - 1)(2 + 5)$ by source							
			1/	$\frac{1}{5} = \frac{1}{3 \times 5}$ by count rea is (2 x 4) x $\frac{1}{3 \times 5}$	$\frac{2 \times 4}{2 \times 4}$ The	thre rectangle, so the a	area of the shaded				
				because they are find	ing 🗧 of 🚽. They can f	urther estimate that th	ne answer must be				
			be	etween $\frac{2}{5}$ and $\frac{4}{5}$ because	$se^{\frac{2}{2}}$ of $\frac{4}{2}$ is more than	of $\frac{4}{2}$ and less than or	the group of $\frac{4}{2}$ .				
				5 5 4	35	2 5	5				
				$\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$	5						
				$2 \frac{1}{3} \frac{1}{15}$		lal and the line see					
				3		lel and the line seg e area is the same					
			$\frac{1}{3}$ quantity as the product of the side								
				1	lengths.						
			Continued	on next page							
			Continueu	on next puge							

Number and Operati	ions—Fraction	s (NF)					
Apply and extend pre-	vious understar	dings of multiplicat	tion and divisio	n to multiply and o	divide fractions co	ntinued	
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others		Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: <b>5.NF.4.</b> continued	Target	5	<ul> <li>Explanations an</li> <li>Carry k</li> <li>1</li> <li>144</li> <li>144</li></ul>	The second seco			following array.
				story problems for ool such as Jing to		0 0	ems.

Number and Operation	ons—Fractio	ns (NF)							
Apply and extend previous understandings of multiplication and division to multiply and divide fractions         Make sense of problems       Reason         Construct viable       Model with         Use appropriate       Attend to precision									
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.		
<u>Standards</u>		Targets		Explanations and Examples					
Students are expected to: 5.NF.5 Interpret mult as scaling (resizing), b	<b>nultiplication</b> Know that scaling (resizing) involves multiplication.			<b>Examples:</b> • $\frac{3}{4} \times 7$ is less than 7 because 7 is multiplied by a factor less					
as scaling (resizing), to a. Comparing the size of product to the size of of on the basis of the size other factor, without p the indicated multiplic b. Explaining why mul- given number by a frac- greater than 1 results i product greater than the number (recognizing multiplication by whol- greater than 1 as a fam case); explaining why multiplying a given nu- fraction less than 1 ress product smaller than the number; and relating to principle of fraction eq- $a/b = (n \times a)/(n \times b)$ to of multiplying $a/b$ by 1 Connections: 5.RI.3; 5.RI.5; 5.W.2b; 5.W.2c; 5.W.2d; 5; 5.SL.2; 5.SL.3;	of a ne factor of the erforming ation. tiplying a ction n a he given e numbers niliar mber by a ults in a he given he uivalence the effect ; 5.W.2a;	Compare the size of a pr size of one factor on the size of the other factor performing the indicate multiplication. For exa- rectangle would have the length of 3. Know that multiplying we numbers and fractions products greater than of one depending upon the Draw a conclusion multi- fraction greater than of in a product greater that number. Draw a conclusion that multiply a fraction by can be written as various ex 2/2, 3/3, etc.) the re- fraction is equivalent. Draw a conclusion that multiply a fraction by product will be smalle given number.	he basis of the c, without ed ample, a 2x3 an area twice whole result in or less than he factors. iplying a ne will result an the given when you one (which ous fractions, sulting when you a fraction, the	• $2\frac{2}{3} \times 8 \text{ m}$ • $2\frac{2}{3} \times 8 \text{ m}$ $2\frac{2}{3} \text{ is all but less}$ • $\frac{3}{4} = \frac{5}{5}$	o the product mus 34  of  7 must be more than most 3 groups of 8 than 24. $\frac{X 3}{X 4}$ because mul- X 4 <i>ing</i> by 1.	at be less than 7.	ps of 8 is 16 and nust be close to,		

Number and Oper Apply and extend			multiplicatio	on and divisio	n to multiply and (	livide fractions		
Make sense of problem and persevere in solvin them.	ns Reason	Construct	-	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.NF.6 Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem. Connections: 5.RI.7; 5.W.2e	Targets Represent word problems involve multiplication of fractions and min numbers ( e.g. b using visual fraction models equations to represent the problem). Solve real world problems involve multiplication of fractions and min numbers.	ing xed y or	amples: • Evan bous • Using • A stu • Mary and area of the • A stu numb The e • First, • Wher • Now • $\frac{1}{3}$ time • $\frac{1}{3}$ time	g a visual, a stud dent can use an Joe determined e school flag? dent can draw an ers to explain th xplanation may I am going to m I multiply $2\frac{1}{4}$ t I have to multip es 2 is $\frac{2}{3}$ . es $\frac{1}{4}$ is $\frac{1}{12}$ .	equation to solve. $\frac{2}{3}$ > that the dimensions o n array to find this pro- te multiplication. This $\begin{bmatrix} 1\\1\\3\\4\end{bmatrix}$ include the following nultiply 2 $\frac{1}{4}$ by 1 and the py 1, it equals 2 $\frac{1}{4}$ .	s into 3 groups and co $6 = \frac{12}{3} = 4$ red is f their school flag near oduct and can also use a student $2\frac{1}{4}$	bounts how many are it roses beded to be $1\frac{1}{3}$ ft. by the his or her understand	

Number and Operation				4 14 <sup>1</sup> 1 1	1		
and persevere in solving a	eason bstractly and uantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
<u>Standards</u> <u>Students are expected to:</u> <b>5.NF.7 Apply and extemprevious understanding</b> division to divide unit fr by whole numbers and numbers by unit fraction <sup>1</sup> Students able to multiply fr in general can develop stradivide fractions in general, reasoning about the relation between multiplication and But division of a fraction b fraction is not a requirement grade. a. Interpret division of a fraction by a non-zero v number, and compute se quotients. For example, story context for (1/3) dit 4, and use a visual fraction multiplication and divisit explain that (1/3) $\div 4 = 1$ because (1/12) $x = 1/3$ .	gs of ractions whole ons. <sup>1</sup> fractions itegies to by onship I division. y a nt at this a unit whole such create a ivided by ion ent. Use	Targets         Know the relationship be multiplication and divi         Interpret division of a ur by a whole number and your answer using the relationship between multiplication and divi by creating story probl visual models, and relat to multiplication, etc.         Interpret division of a winumber by a unit fracti justify your answer usi relationship between multiplication and divi by representing the quater a visual fraction model Solve real world probler involving division of u fractions by whole num other than 0 and division whole numbers by unit using strategies such as fractions models and ended such as the such	sion. hit fraction d justify sion, and ems, using tionship hole on and ng the sion, and otient with l. ns nit nbers on of a fractions s visual	divisors and unit fi with unit fraction of their understanding are in a whole, and involving equal gr group/share. In six to divide into and methods of dividir <b>Example</b> : Knowir many/much in eac • Four student to share. H pan of brow The diagram show share equaling 1/1	lents experience d raction dividends divisors and whol g of the meaning l their understand oups or shares and th grade, they will by more complex ng by fractions. Ing the number of g h group/share nts sitting at a tab ow much of a par whies equally? The sthe 1/3 pan divi 2 of the pan. $\frac{1}{12}$	(fractions with a set number dividen of fractions, how ing of multiplicat d the number of o ll use this foundat fractions and dev groups/shares and le were given 1/3 n will each studen ded into 4 equal s	ional understanding relop abstract finding how of a pan of brownies t get if they share the
Continued on next page				Continued on next page	ge		

Number and Operat	ions—Fractio	ns (NF)					
Apply and extend pre	vious understai	ndings of multiplication	on and divisio	n to multiply and o	divide fractions co	ntinued	
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.NF.7 continued b. Interpret division of number by a unit fract compute such quotient example, create a story of $4 \div (1/5)$ , and use a visis fraction model to show the quotient. Use the relations between multiplications division to explain that $= 20$ because $20 \times (1/5)$ c. Solve real world pro- involving division of uf- fractions by non-zeron numbers and division numbers by unit fract by using visual fractions and equations to repro- problem. For examples much chocolate will ex- person get if 3 peoples lb. of chocolate equallist many 1/3 cup servings cups of raisins? Connections: 5.RI.3; 5.RI. 5.W.2c; 5.SL.6	of a whole tion, and hts. For context for ual the onship and $4 \div (1/5)$ = 4. oblems init whole of whole ions, e.g., n models esent the c, how each share 1/2 ly? How s are in 2	<u>argets</u>	Examples groups/sha • Ar Ho A diagram fifths in or • Ho equ	hgelo has 4 lbs of p ow many friends c in for $4 \div 1/5$ is sho ne whole, there multiple 1 lb. of peanuts 1  lb. of peanuts $\frac{1}{5}$ lb. ow much rice will ually? $3 = \frac{3}{6} \div 3 = \frac{1}{6}$ A student may the determine that each	peanuts. He wants an receive 1/5 lb o wn below. Studer ust be 20 fifths in	to give each of h of peanuts? nts explain that sin 4 lbs. 3 people share 1/ d cut it into 3 equ s 1/6.	is friends 1/5 lb. nce there are five /2 lb of rice al groups then

Measurement and D	ata (MI	D)							
Convert like measurement units within a given measurement system									
Make sense of problems and persevere in solving them.		actly and arguments and critique math		Model with mathematics.		Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards         Students are expected to:         5.MD.1 Convert and         different-sized star         measurement units         within a given         measurement system         (e.g., convert 5 cm         0.05 m), and use the         conversions in solver         multi-step, real wor         problems.	Reason abstractly and quantitatively.Construct viable arguments and critique the reasoning of others.Mode mathong ndardTargets Recognize units of measurement within the same system.Mode mathong ndardTargets Recognize units of 			nge nent	In fif mea actu the exp mea	al conversions, th converted amount lain their reasonin	build on their prid determine equiva ey examine the un will be more or la g. They use sever converting metric	lent measurement nits to be converte ess units than the al strategies to con c measurement, st	elated s. Prior to making d, determine if original unit, and

Measurement and Da	ata (MD)							
Represent and interpre	et data							
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	ractly and arguments and critique mat ntitatively. the reasoning of others.		del with thematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.MD.2 Make a line p display a data set of measurements in frac- of a unit (1/2, 1/4, 1/8) operations of fraction this grade to solve pr involving information presented in line plot example, given different measurements of liqui identical beakers, find amount of liquid each would contain if the to amount in all the beak were redistributed equi-	plot to ctions 3). Use ns for coblems n Sts. For ent wid in d the h beaker fotal kers wally.	Targets identify benchmark fractions (1/2, 1/4, 1/8) Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Solve problems involvin information presented line plots which use fractions of a unit (1/2, 1/4, 1/8) by adding, subtracting, multiplyin and dividing fractions.	ng in g,	Student	akers. Then the su	Liquid in x x x x x x x x x x x x x x x x x x x	Beakers Beakers $\frac{3}{4}$ 1 $\frac{3}{4}$ 1 $\frac{3}{4}$ 1 $\frac{1}{1}$	ers in 10 beakers. d would each ns. They use number of liters in

Measurement and Da	ata (MD	))							
Geometric measureme	ent: und	lerstand	concepts of volume a	nd relate volu	ume to multiplicat	ion and to addition	n		
Make sense of problems	Reason		Construct viable	Model with	Use appropriate	Attend to precision.	Look for and make	Look for and	
and persevere in solving them.	abstract quantita		arguments and critique the reasoning of others.	mathematics.	tools strategically.		use of structure.	express regularity in repeated reasoning.	
<u>Standards</u>		<u>Targets</u>			Explanations and Examples				
Students are expected to: 5.MD.3ab Recognize		Recognize that volume is			1 1		e restricted to liqui		
volume as an attribu		the measurement of the			-	-	-	that a 1-unit by 1-	
solid figures and	space inside a solid unce-		-			heasuring volume.			
understands concept	annensionar ingare.					ht of 1 unit and is nent of 3 (e.g., $in^3$ )			
volume measuremen						of powers of 10 in			
<ul> <li>a. A cube with side left 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be ut to measure volume.</li> <li>b. A solid figure which can be packed withor gaps or overlaps usin unit cubes is said to have a volume of <i>n</i> cubic to the connections: <i>5.NBT.2; 5.R 5.W.2d; 5.SL.1c; 5.SL.1d</i></li> </ul>	e 1sed ch ut ng <i>n</i> have units.	and i volu dime Recog pack overl (n) "	s used to measure me of three- nsional shapes. nize any solid figure ed without gaps or aps and filled with unit cubes" indicates otal cubic units or	system. I developi would be needed to	Models of cubic in ng an image of a c	nches, centimeters cubic unit. Studen e classroom or how	t's estimate how n w many cubic cent	are helpful in nany cubic yards	

Measurement and Da	Measurement and Data (MD)									
Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition										
Make sense of problems and persevere in solving them.		,	Construct viable arguments and critique the reasoning of others.	Model with mathemati		Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.	
Standards Students are expected to: 5.MD.4 Measure vol by counting unit cub using cubic cm, cubi cubic ft., and improv units. Connections: 5.MD.3; 5.R	ense of problems severe in solvingReason abstractly and quantitatively.Construct viable arguments and critic the reasoning of othrds rds re expected to:Targets Measure volumes ounting unit cubes, cubic cm, cubic in., ft., and improvisedConstruct viable arguments and critic the reasoning of oth					ect appropriate un on between which of a gym and the v it using any unit a y these ideas by fi	tits to measure voluits to measure voluits are more ap volume of a box of a length (e.g., the illing containers way also use drawing	its are used to mea lume. For example propriate for meas f books. They can the length of their p with cubic units (w gs or interactive co	e, they make a suring the also improvise a bencil). Students ooden cubes) to	
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<b>Measurement and Dat</b>	Measurement and Data (MD)							
Geometric measuremen	: understan	d concepts of volu	ime and relate vo	lume to multiplicat	ion and to additior	ı		
Geometric measuremen Make sense of problems and persevere in solving	t understand eason bstractly and uantitatively.	Construct viable arguments and criti the reasoning of oth gular prism. () the three sions in any () calculate e. () tative and ative properties). () volume la for a rectangle by () ring volume filled with cubes () une by () lying the height area of the base, en multiplying ge lengths (xH).	que mers.     Model with mathematics.       Explanations and Students need mul looking at the reformula (volume other prisms. Stuusing factors to it Examples:       • When give 24 cubic       Length       1       2       4       8	Use appropriate tools strategically.	Attend to precision. heasure volume by fil total volume and the base times the height ve property of multip prisms with a given r make as many rectang e prisms and record p of concrete needed to	Look for and make use of structure. ling rectangular prism area of the base. The ) and explore how thi lication and decompo- number of cubic units gular prisms as possib possible dimensions.	y derive the volume s idea would apply to osition of numbers ole with a volume of	
Represent threefold whole-number procedur as volumes, e.g., to represent the associative property of multiplication. Continued on next page	es right r with w side le	volume of a ectangular prism whole number ngths by g it with unit		wner is building a swir ol. The design of the p		lustration below.	ume of water needed to	

<b>Measurement and D</b> Geometric measurem		concepts of volume a	nd relate volun	ne to m	ultinlicatio	n and to additio	on continued	
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	r	propriate	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.MD.5 continued b. Apply the formula and V=B x h for record prisms to find volume rectangular prisms of number lengths in the solving real world ate mathematical problection c. Recognize volume Find volumes of solicies composed of two notest right rectangular prisms adding the volumess overlapping parts, ate technique to solve records problems. Connections: 5.RI.3; 5.W.2c; 5.SL.3	tangular nes of right with whole- he context of nd ems. e as additive. d figures n-overlapping risms by of the non- applying this eal world	Apply the followin right rectangular whole number ed context of real w problems: Volume = length x Volume = area of 1 Recognize volume	ng formulas to prisms having lge lengths in t orld mathemat width x heigh base x height. as additive. roblems by blid figure into bing right	the fical nt.	Explanation See above	ns and Examples		

Geometry (G)							
Graph points on the co	ordinate plan	e to solve real-world a	nd mathema	tical problems			
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.G.1 Use a pair of perpendicular numb called axes, to define coordinate system, w intersection of the lin origin) arranged to c with the 0 on each lin given point in the pla located by using an o pair of numbers, call coordinates. Underst that the first number indicates how far to to from the origin in the direction of one axis, the second number in how far to travel in t direction of the secon with the convention of names of the two axe the coordinates corre (e.g., x-axis and x- coordinate). Connections: 5.RI.4; 5.W.2	TaraTarDeaLorith thecurith thecunes (theIdephe and asianeReorderedthled itsthtraveleandndicateshendnd axis,that thesandespond	The reasoning of others. <u>rgets</u> fine the coordinate ystem entify the x- and y-axis cate the origin on the oordinate system entify coordinates of a oint on a coordinate ystem cognize and describe ne connection betwee ne ordered pair and th - and y-axis (from the rigin)	Examp • • • • • • • • • • • • •	tions and Examples tions and Examples les: Students can use a locate the coordina walking 5 units ald and then walking to ordered pair name Graph and label th $\circ$ A (0,0) $\circ$ B (5,1) $\circ$ C (0,6) $\circ$ D (2.5,6) $\circ$ E (6,2) $\circ$ F (4,1) $\circ$ G (3,0)	ate point $(5, 3)$ by ong the x axis to f up 3 units for the s s a point in the pla	starting at the original the first numb second number in ane. (5,5) (5,3) (5,3) (5,3) (5,3)	to physically gin point (0,0), er in the pair (5), the pair (3). The

Geometry (G)							
Graph points on the	coordinate pla	ne to solve real-wor	ld and math	ematical problen	15		
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.G.2 Represent real world and mathema problems by graphin points in the first quadrant of the coordinate plane, an interpret coordinate values of points in th context of the situati	tical quad tical Representation ng math by gr first d Interpresentation of point ne conter	points in the first	Examples • Sa • Sa • O • Us wo Earnings (S 20 16 U) 12 Sa • Us wo • Us vo • Us	ra has saved \$20. If Sara saves all working 3 hours Create a graph th worked and the a	of her money, how ? 5 hours? 10 hou hat shows the relate amount of money mation do you kn to determine how burs.	w much will she h rs? tionship between she has saved. ow from analyzin	have after the hours Sara ag the graph?

Geometry (G)							
Classify two-dimension	nal figures iı	to categories based on t	heir properti	es			
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
them. <u>Standards</u> <u>Students are expected to:</u> <b>5.G.3 Understand th</b> <b>attributes belonging</b> <b>category of two-</b> <b>dimensional figures a</b> <b>belong to all</b> <b>subcategories of that</b> <b>category. For examp</b> <b>all rectangles have for</b> <b>right angles and squa</b> <b>are rectangles, so all</b> <b>squares have four rig</b> <b>angles.</b> Connections: <i>5.RI.3</i> ; <i>5.RI.4</i> <i>5.RI.5</i> ; <i>5.W.2b</i> ; <i>5.W.2c</i> ; <i>5.N</i> <i>5.SL.1</i>	at di Tara Rec at di to a be thalso on Rec di le, cla bur tha ares su ca ght ca	- I	Geometric congruen propertie Example: • If t rec • A 0 0 0 0 0	the opposite sides etangles are paralle sample of question A parallelogram What types of qu Regular polygon or draw some reg All rectangles ha they are also rect	ngles (type, meas oint and line). on a parallelogram elograms ns that might be p has 4 sides with b adrilaterals are pa s have all of their gular polygons. twe 4 right angles. tangles. True or F 2 sides parallel so	urement, congrues m are parallel and osed to students in poth sets of opposi- arallelograms? sides and angles of Squares have 4 ri alse? it must be a paral	endicular, nt), and congruent, then nclude: ite sides parallel. congruent. Name ght angles so

Geometry (G)							
Classify two-dimension	nal figures into	categories based on t	heir propertie	es			
Make sense of problems and persevere in solving them.	Reason abstractly and quantitatively.	Construct viable arguments and critique the reasoning of others.	Model with mathematics.	Use appropriate tools strategically.	Attend to precision.	Look for and make use of structure.	Look for and express regularity in repeated reasoning.
Standards Students are expected to: 5.G.4 Classify two- dimensional figures in hierarchy based on properties. Connections: 5.RI.5; 5.W.2 5.W.2d; 5.SL.1; 5.SL.2; 5.SL 5.SL.6	n a two-o based Analyz dime 2c; hiera L.3; hiera figur and/o	nize the hierarchy of dimensional shapes l on their attributes. ze properties of two- nsional figures in to place into a	Properties of Properties of Properties A tripological and the second	right triangle can be scalene triangle can angles can be classi- les Right: The triangle Acute: The triangle 90°. Obtuse: The triang and less than 180° s Equilateral: All sid Isosceles: At least Scalene: No sides quadrilateral	lel, perpendicular, c es of angles, congru both scalene and is be right, acute and ified by: e has one angle that e has exactly three gle has exactly one des of the triangle a two sides of the tri of the triangle are t polygon	ent sosceles, but not eq obtuse. t measures 90°. angles that measures angle that measures re the same length. angle are the same	uilateral. e between 0° and s greater than 90°

Standards for Mathematical Practice (MP)		
<u>Standards</u> Students are expected to:	<u>Mathematical Practices</u> are listed throughout the grade level document in the 2nd column to reflect the need to connect the mathematical practices to mathematical content in instruction.	Explanations and Examples
<b>5.MP.1.</b> Make sense of problems and persevere in solving them.		Students solve problems by applying their understanding of operations with whole numbers, decimals, and fractions including mixed numbers. They solve problems related to volume and measurement conversions. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, "What is the most efficient way to solve the problem?", "Does this make sense?", and "Can I solve the problem in a different way?".
<b>5.MP.2.</b> Reason abstractly and quantitatively.		Fifth graders should recognize that a number represents a specific quantity. They connect quantities to written symbols and create a logical representation of the problem at hand, considering both the appropriate units involved and the meaning of quantities. They extend this understanding from whole numbers to their work with fractions and decimals. Students write simple expressions that record calculations with numbers and represent or round numbers using place value concepts.
<b>5.MP.3.</b> Construct viable arguments and critique the reasoning of others.		In fifth grade, students may construct arguments using concrete referents, such as objects, pictures, and drawings. They explain calculations based upon models and properties of operations and rules that generate patterns. They demonstrate and explain the relationship between volume and multiplication. They refine their mathematical communication skills as they participate in mathematical discussions involving questions like "How did you get that?" and "Why is that true?" They explain their thinking to others and respond to others' thinking.
<b>5.MP.4.</b> Model with mathematics.		Students experiment with representing problem situations in multiple ways including numbers, words (mathematical language), drawing pictures, using objects, making a chart, list, or graph, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed. Fifth graders should evaluate their results in the context of the situation and whether the results make sense. They also evaluate the utility of models to determine which models are most useful and efficient to solve problems.

Standards for Mathematical Practice (MP)			
<u>Standards</u> Students are expected to:	<u>Mathematical Practices</u> are listed throughout the grade level document in the 2nd column to reflect the need to connect the mathematical practices to mathematical content in instruction.	Explanations and Examples	
<b>5.MP.5.</b> Use appropriate tools strategically.		Fifth graders consider the available tools (including estimation) when solving a mathematical problem and decide when certain tools might be helpful. For instance, they may use unit cubes to fill a rectangular prism and then use a ruler to measure the dimensions. They use graph paper to accurately create graphs and solve problems or make predictions from real world data.	
<b>5.MP.6.</b> Attend to precision.		Students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students use appropriate terminology when referring to expressions, fractions, geometric figures, and coordinate grids. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, when figuring out the volume of a rectangular prism they record their answers in cubic units.	
<b>5.MP.7.</b> Look for and make use of structure.		In fifth grade, students look closely to discover a pattern or structure. For instance, students use properties of operations as strategies to add, subtract, multiply and divide with whole numbers, fractions, and decimals. They examine numerical patterns and relate them to a rule or a graphical representation.	
<b>5.MP.8.</b> Look for and express regularity in repeated reasoning.		Fifth graders use repeated reasoning to understand algorithms and make generalizations about patterns. Students connect place value and their prior work with operations to understand algorithms to fluently multiply multi-digit numbers and perform all operations with decimals to hundredths. Students explore operations with fractions with visual models and begin to formulate generalizations.	